

Algebra Prelim part A

January 9, 2017

Directions: You have 90 minutes.

- A1.** Fix a field \mathbf{F} . Suppose J is a Jordan block of size n with eigenvalue $\lambda \in \mathbf{F}$. Establish the shape of the Jordan decomposition of J^2 .
- A2.** Classify the groups of order 105 up to isomorphism.
- A3.** Suppose R is a PID. Say what the following assertion means, and prove it. “Any two nonzero elements x, y of R have a least common multiple.”